

## Thermodynamic Laws

**Zeroth Law:** When two systems are in thermal equilibrium with a third system, they must be in thermal equilibrium with each other.

**First Law (closed system):**  $Q = m\Delta u + W / J$

Heat entering a system can either increase temperature (internal energy) or be used to perform work on the surroundings. It is the law of energy conservation, i.e., energy cannot be created or destroyed.

**Second Law (isolated system):**  $m\Delta S_{total} \geq 0$

The entropy change of any system and its surroundings, considered together, is positive, and approaches zero for any process that approaches reversibility. It is considered the fundamental law of natural science.

**The two classical statements of the Second Law:**

**Clausius statement:** It is impossible to construct a device that operates in a cycle and produces no effect other than the transfer of heat from a cooler body to a hotter body.

**Kelvin-Plank statement:** It is impossible to construct a device that operates in a cycle and produces no effect other than the raising of a weight and the exchange of heat with a single reservoir.

**Third Law:** It is impossible to cool a body down to absolute zero.

## Thermodynamic Laws (simplified)

**First Law:** You can't win, you can only break even.

**Second Law:** You can only break even at absolute zero.

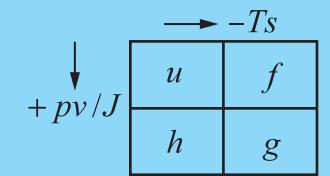
**Third Law:** You can never reach absolute zero.

## Thermodynamic Equations

**Ideal Gas Law:**  $pV = nRT = NkT; V = mv; n = m/M; k = R/N_A$

**Helmholtz Function:**  $f = u - Ts$

**The four thermodynamic potentials:**



**Gibbs Function:**  $g = h - Ts$

$$\text{Equation of State: } p = -J \left( \frac{\partial f}{\partial v} \right)_T + pv/J$$

**Enthalpy:**

$$h = u + pv / J = \int \left[ c_v + \frac{v}{J} \left( \frac{\partial p}{\partial T} \right)_v \right] dT + \frac{1}{J} \int \left[ v \left( \frac{\partial p}{\partial v} \right)_T + T \left( \frac{\partial p}{\partial T} \right)_v \right] dv$$

$$\text{Entropy: } s = - \left( \frac{\partial f}{\partial T} \right)_v = - \left( \frac{\partial g}{\partial T} \right)_p = \int \frac{c_v}{T} dT + \frac{1}{J} \int \left( \frac{\partial p}{\partial T} \right)_v dv$$

$$\text{Isochoric Specific Heat: } c_v = \left( \frac{\partial u}{\partial T} \right)_v = T \left( \frac{\partial s}{\partial T} \right)_v = c_v + \frac{1}{J} \int_{\infty}^v T \left( \frac{\partial^2 p}{\partial T^2} \right)_v dv$$

$$\text{Isobaric Specific Heat: } c_p = \left( \frac{\partial h}{\partial T} \right)_p = T \left( \frac{\partial s}{\partial T} \right)_p = c_v - \frac{T \left( \frac{\partial p}{\partial T} \right)_v^2}{J \left( \frac{\partial p}{\partial v} \right)_T}$$

**Specific Heat Ratio:**  $\gamma = c_p/c_v = \kappa/\kappa_s$

**Velocity of Sound:**

$$a = v \sqrt{J g_c \gamma \left( \frac{\partial^2 f}{\partial v^2} \right)_T} = v \sqrt{-g_c \gamma \left( \frac{\partial p}{\partial v} \right)_T} = v \sqrt{g_c \left[ T \left( \frac{\partial p}{\partial T} \right)_v^2 - \left( \frac{\partial p}{\partial v} \right)_T \right]}$$

### Nomenclature

	I-P	S-I
a	velocity of sound	ft/sec
c <sub>p</sub>	isobaric specific heat	Btu/lb <sub>m</sub> °R
c <sub>v</sub>	isochoric specific heat	Btu/lb <sub>m</sub> °R
f	Helmholtz function	kJ/kg
g	Gibbs function	Btu/lb <sub>m</sub>
g <sub>c</sub>	gravitational conversion factor	kJ/kg
h	enthalpy	Btu/lb <sub>m</sub>
J	Joule's constant	778.16926 ft-lb <sub>t</sub> /Btu
m	mass	lb <sub>m</sub>
M	molecular weight	---
N	no. of molecules	---
n	no. of moles	lb mol
p	pressure	lb/ft <sup>2</sup>
Q	heat	Btu
s	entropy	Btu/lb <sub>m</sub> °R
T	temperature	°R
u	internal energy	Btu/lb <sub>m</sub>
v	specific volume	ft <sup>3</sup> /lb <sub>m</sub>
V	volume	m <sup>3</sup>
W	work	ft-lb <sub>t</sub>
κ	isothermal compressibility	ft <sup>2</sup> /lb <sub>t</sub>
κ <sub>a</sub>	adiabatic compressibility	(kPa) <sup>-1</sup>
γ	specific heat ratio	---

Superscript: 0 = heat capacity at zero pressure

(Physical Constants on reverse side.)

## Carrying Capacity of Refrigeration Lines - Tons of Refrigeration

R-22	Line Size	Suction Lines				Liquid Lines				Discharge Lines			
		Velocity = 1500 fpm				Velocity = 150 fpm				Velocity = 150 fpm			
	Type L Copper OD (Inches)	Suction Temperature (°F)	Δt = 1°F Δp = 0.39 psi	Δp = 0.57 psi	Δp = 0.81 psi	Δp = 1.1 psi	Suction Temperature (°F)	Δt = 1°F, Δp = 1.9 psi	Δt = 1°F, Δp = 3.0 psi	Suction Temperature (°F)	Δt = 1°F, Δp = 2.0	Δt = 1°F, Δp = 2.0	
3/8	0.09	0.14	0.22	0.33	0.43	0.53	0.02	0.04	0.06	0.09	0.14	0.22	0.33
1/2	0.17	0.27	0.45	0.64	0.86	1.05	0.10	0.15	0.23	0.35	0.58	0.25	0.37
5/8	0.27	0.44	0.68	1.03	1.11	1.29	0.11	0.18	0.29	0.43	0.68	1.36	0.48
7/8	0.56	0.91	1.42	2.13	3.0	0.49	0.76	1.13	1.45	1.53	1.13	11.9	4.93
1-1/8	0.95	1.55	2.42	3.63	6.61	0.99	1.54	2.30	2.47	2.60	2.31	24.3	9.96
1-3/8	1.45	2.36	3.69	5.53	1.06	1.74	2.70	4.02	3.76	3.96	40.4	42.6	17.3
1-5/8	2.05	3.35	5.22	7.83	1.69	2.76	4.28	6.37	5.33	56.1	64.1	76.6	27.4
2-1/8	3.57	5.82	9.07	13.6	3.54	5.76	8.92	13.2	9.26	97.6	134	141	56.5
2-5/8	5.51	8.88	14.0	21.0	6.29	10.2	15.8	23.4	143	150	237	250	99.7
3-1/8	7.87	12.8	20.0	30.0	10.1	16.4	25.3	37.5	204	215	379	400	159
3-5/8	10.6	17.3	27.0	40.6	15.0	24.4	37.7	55.7	276	291	565	595	235
4-1/8	13.8	22.5	35.1	52.7	21.3	34.5	53.2	78.7	359	378	798	841	331
4-5/8	21.6	35.1	54.7	82.2	38.3	61.9	95.4	141	559	589	1430	1510	580
5-1/8	31.0	50.5	78.7	118	61.7	99.8	154	227	803	846	2310	2430	947

R-134a	Line Size	Suction Lines				Liquid Lines				Discharge Lines			
		Velocity = 1500 fpm				Velocity = 150 fpm				Velocity = 150 fpm			
	Type L Copper OD (Inches)	Suction Temperature (°F)	Δt = 1°F Δp = 0.33 psi	Δp = 0.49 psi	Δp = 0.70 psi	Suction Temperature (°F)	Δt = 1°F, Δp = 1.3 psi	Δt = 1°F, Δp = 2.2 psi	Suction Temperature (°F)	Δt = 1°F, Δp = 2.2 psi	Δt = 1°F, Δp = 2.2 psi		
3/8	0.08	0.13	0.21	0.02	0.03	0.06	2.11	2.29	0.68	0.73	0.28	0.30	0.42
1/2	0.15	0.25	0.40	0.05	0.13	0.17	4.37	1.63	1.77	1.77	0.66	0.72	1.00
5/8	0.24	0.40	0.64	0.09	0.16	0.25	6.47	7.02	3.10	3.36	1.23	1.35	1.98
7/8	0.50	0.84	1.33	0.25	0.42	0.67	13.4	14.6	8.27	8.97	3.23	3.56	4.48
1-1/8	0.86	1.43	2.27	0.51	0.86	1.36	22.9	24.8	16.9	18.3	6.54	7.20	10.4
1-3/8	1.31	2.17</td											

# Refrigeration Engineer Quick Reference



## Fluid Flow Equations

Bernoulli equation:

$$\frac{P_1 g_c}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2 g_c}{\gamma} + \frac{V_2^2}{2g} + z_2; \quad \gamma = \rho g$$

Reynolds Number:

$$R_e = \frac{vD}{\nu} = \frac{vD\rho}{\mu g_c}$$

Colebrook's equation:

$$\frac{1}{\sqrt{f}} = -2 \log_{10} \left[ \frac{\epsilon/D}{3.7} + \frac{2.51}{R_e \sqrt{f}} \right]$$

Darcy-Weisbach equation:

$$h_f = f \frac{L_e V^2}{D 2g}$$

Orifice equation (incompressible flow):

$$m = C_f A_o \sqrt{2 g_c p \Delta p}; R_e > 250$$

Orifice equation (vapor flow):

$$m = C_f A_o \sqrt{\frac{2k}{k-1} p_u g_c p_u \left( \frac{p_d}{p_u} \right) \left[ 1 - \left( \frac{p_d}{p_u} \right)^{(k-1)/k} \right]}$$

where  $\frac{p_d}{p_u} >$  critical pressure ratio

Critical pressure ratio:

$$\frac{p_d}{p_u} = \left( \frac{2}{k+1} \right)^{k/(k-1)}$$

## Nomenclature

### I-P

### S-I

$A_o$	orifice area	ft <sup>2</sup>	m <sup>2</sup>
$C_f$	flow coefficient	---	---
$D$	diameter	ft	m
$f$	friction factor	---	---
$g_c$	gravitational conversion factor	32.174 lb <sub>m</sub> ·ft/lb <sub>f</sub> ·sec <sup>2</sup>	1.0
$k$	specific heat ratio	---	---
$h_f$	head loss due to friction	ft	m
$L_e$	equivalent length	ft	m
$m$	mass flow rate	lb <sub>m</sub> /sec	kg/sec
$p$	pressure	lb <sub>f</sub> /ft <sup>2</sup>	Pa
$R_e$	Reynold's Number	---	---
$v$	velocity	ft/sec	m/sec
$z$	height	ft	m
$\epsilon$	effective roughness	ft	m
$\gamma$	specific weight	lb <sub>m</sub> /ft <sup>2</sup> ·sec <sup>2</sup>	N/m <sup>3</sup>
$\mu$	absolute viscosity	lb <sub>f</sub> ·sec/ft <sup>2</sup>	Pa·sec
$\nu$	kinematic viscosity	ft <sup>2</sup> /sec	m <sup>2</sup> /sec
$\rho$	density	lb <sub>m</sub> /ft <sup>3</sup>	kg/m <sup>3</sup>

Subscripts:  $u$  = upstream;  $d$  = downstream

## Physical Constants

### I-P

### S-I

$g$	standard acceleration due to gravity	32.1740 ft/sec <sup>2</sup>	9.80665 m/sec <sup>2</sup>
$k$	Boltzmann's constant	5.657308x10 <sup>-24</sup> ft-lb <sub>f</sub> /°R	1.380650x10 <sup>-26</sup> kJ/K
$N_A$	Avogadro's constant	2.73159766x10 <sup>26</sup> / lb mol	6.02214199x10 <sup>26</sup> / kg mol
$R$	universal gas constant	1545.349 ft-lb <sub>f</sub> /lb mol·°R	8.314471 kJ/kg mol·°K

## Refrigerant Data

ASHRAE Number	Chemical Name	Sporlan Letter Designation	Color Designation (PMS No.) <sup>1</sup>	ASHRAE 34 Safety Group	CAS Registry Number	Critical Values <sup>2</sup>			Molecular Weight
						Temperature (°F)	Pressure (psia)	Specific Vol (ft <sup>3</sup> /lb <sub>m</sub> )	
R-10	tetrachloromethane (carbon tetrachloride)	H	Orange (021)	A1	56-23-5	542.03	661.37	0.0287	153.82
R-11	trichlorodifluoromethane	F	White (N/A)	A1	75-69-4	388.33	639.27	0.0289	137.37
R-12	dichlorodifluoromethane			A1	353-59-3	232.55	598.89	0.0284	120.91
R-12B1	bromochlorodifluoromethane (halon 1211)	E	Light Blue (297)	A1	75-72-9	308.84	594.94	0.0225	165.36
R-13B1	chlorotrichlorofluoromethane (halon 1301)	T	Pinkish-Red/Coral (177)	A1	75-63-8	83.71	562.31	0.0275	104.46
R-14	tetrafluoromethane (carbon tetrafluoride)		Yellow-Brown/Mustard (124)	A1	75-73-0	152.60	574.90	0.0215	146.91
R-20	trichloromethane (chloroform)			A1	67-66-3	504.23	794.81	0.0324	119.38
R-21	dichlorodifluoromethane			B1	75-43-4	353.21	751.30	0.0306	102.92
R-22	chlorodifluoromethane	V	Light Green (352)	A1	75-45-6	205.06	723.74	0.0306	86.47
R-22B1	bromodifluoromethane (halon 1201)	G	Light Blue-Gray (428)	A1	1511-62-2	281.89	744.33	0.0204	130.92
R-23	trifluoromethane			A1	75-46-7	78.66	701.40	0.0305	70.01
R-30	dichloromethane (methylene chloride)			B2	75-09-2	455.27	881.83	0.0357	84.93
R-31	chlorofluoromethane				593-70-4	305.17	744.20	0.0371	68.48
R-32	difluoromethane (methylene fluoride)			A2	75-10-5	172.59	838.61	0.0378	52.02
R-40	chloromethane (methyl chloride)			B2	74-87-3	289.49	965.95	0.0446	50.49
R-41	fluoromethane (methyl fluoride)				593-53-3	111.43	855.29	0.0506	34.03
R-50	methane			A3	74-82-8	-116.70	666.40	0.0988	16.04
R-110	hexachloroethane				67-72-1	808.3	571	0.0284	236.74
R-113	1,1,2-trichloro-1,2,2-trifluoroethane			B1	76-13-1	417.31	492.00	0.0286	187.37
R-114	1,2-dichloro-1,1,2-tetrafluoroethane	B	Dark Purple/Violet (266)	A1	76-14-2	294.22	472.39	0.0276	170.92
R-115	chloropentafluoroethane			A1	76-15-3	175.91	452.52	0.0261	154.47
R-116	hexafluoroethane			A1	76-16-4	67.78	441.20	0.0256	136.01
R-123	2,2-dichloro-1,1,1-trifluoroethane	M	Dark Grey (424)	B1	306-83-2	362.63	531.10	0.0291	152.93
R-124	2-chloro-1,1,1,2-tetrafluoroethane		Light Blue-Gray (428)	A1	2837-89-0	252.10	525.66	0.0286	136.48
R-125	pentanofluoroethane			A1	354-33-6	151.12	526.34	0.0280	120.02
R-130	1,1,2-tetrachloroethane			A1	79-34-5	730.5	847.0		167.85
R-134a	1,1,1,2-tetrafluoroethane	J	Light Blue (297)	A1	811-97-2	213.91	588.75	0.0313	102.03
R-141b	1,1-dichloro-1-fluoroethane				1717-00-6	399.56	616.41	0.0348	116.95
R-142b	1-chloro-1,1-difluoroethane			A2	75-68-3	278.78	597.99	0.0368	100.50
R-143a	1,1,1-trifluoroethane			A2	420-46-2	163.20	547.60	0.0370	84.04
R-150	1,2-dichloroethane			A1	107-06-2	559.1	778.9	0.0364	98.96
R-152a	1,1-dichloroethane			A2	75-37-6	235.87	655.10	0.0435	66.05
R-160	chloroethane (ethyl chloride)			A2	75-00-3	369.1	764		64.51
R-160B1	ethyl bromide (halon 2001)				74-96-4	447.3	903.6		108.96
R-161	fluorooethane (ethyl fluoride)				353-36-6	216.0	682		48.06
R-170	ethane			A3	74-94-0	89.92	706.59	0.1120	30.07
R-227ea	1,1,1,2,3,3-heptafluoropropane	K		A3	431-89-0	217.04	432.21	0.0276	170.03
R-236ea	1,1,1,2,3,3-hexafluoropropane			A3	431-63-0	282.72	507.92	0.0285	152.04
R-245ea	1,1,2,2,3-pentafluoropropane			A1	679-66-7	345.56	569.27	0.0306	134.05
R-C270	cyclopropane			A1	460-73-11	309.29	527.94	0.0310	134.05
R-290	propane			A3	75-19-4	257.27	809.23	0.0617	42.08
R-318	octafluorocyclobutane			A1	115-25-3	239.41	402.84	0.0258	200.04
R-600	n-butane</td								